## Explain volume formulas and use them to solve problems (Standards G.GMD.1, 3)

Standard II.G.GMD.1: Give an informal argument for the formulas for the circumference of a circle, area of a circle, volume of a cylinder, pyramid, and cone. Informal arguments for area formulas can make use of the way in which area scale under similarity transformations: when one figure in the plane results from another by applying a similarity transformation with scale factor $k$, its area is $k^{2}$ times the area of the first. Use dissection arguments, Cavalieri's principle, and informal limit arguments.

## Concepts and Skills to Master

- Develop the formulas for the circumference of a circle, area of a circle, and volume of a cylinder, pyramid, and cone using a variety of arguments.
- Consider why the various formulas work, using drawings and models as needed.
- Use similarity to define $\pi$ and develop the formula for the circumference of a circle.
- Use a limit argument to develop the area of a circle.
- Use Cavalier's principle to explain why the formulas for the volume of a cylinder, pyramid, and cone work.
- Relate the volumes among various solids with the same dimensions.

| Related Standards: Current Course | Related Standards: Future Courses |
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| G.C.4, 6.G.2, 7.G.4, 8.G.9 |  |

## Support for Teachers

## Critical Background Knowledge

- Use mathematical language and a logical progression of ideas to present an argument.

Academic Vocabulary
cylinder, right prism, pyramid, cone, dissection argument, Cavalieri's principle, limit argument

## Resources

Curriculum Resources: http://schools.utah.gov/curr/mathsec/Core/HighSchoolCurriculum.aspx

## Explain volume formulas and use them to solve problems (Standards G.GMD.1, 3)

| Standard II.G.GMD.3: Use volume formulas for cylinders, pyramids, cones, and spheres to solve problems. Informal arguments for volume |
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| formulas can make use of the way in which volume scale under similarity transformations: when one figure results from another by applying |
| a similarity transformation, volumes of solid figures scale by $k_{3}$ under |
| a similarity transformation with scale factor $k$. |
| Concepts and Skills to Master |
| - Find the volume of cylinders, pyramids, cones, and spheres in contextual problems. |
| - Apply volume formulas to suggest solutions to real-world problems involving geometric solids. |
| Related Standards: Current Course |
| 7.G.6, 8.G.9 |

## Support for Teachers

## Critical Background Knowledge

- Formulas for the volumes of cones, cylinders, and spheres (8.G.9).


## Academic Vocabulary

pyramid, cylinder, cone, sphere, volume, length, width, height, base, radius, $\pi$.

## Resources

Curriculum Resources: http://schools.utah.gov/curr/mathsec/Core/HighSchoolCurriculum.aspx

